

# Revisiting Antlia 2's Effect on the Outer Disk

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## Abstract

Antlia 2 is the lowest surface-brightness satellite galaxy to our Milky Way that was discovered using data by the Gaia Mission, in the second data release (DR-2). Previous publications suggest that Antlia 2 may be responsible for observed large perturbations in the outer HI disk of our Galaxy. Earlier calculations used Gaia DR-2 proper motion measurements to constrain the stars within Antlia 2 and determine its orbit. It was found that low pericenter orbits ( $\sim 10$  kpc) produce disturbances that match the observed perturbations. We use newly calculated Gaia EDR3 proper motions of Antlia 2 to compute pericenter distributions. We also independently recalculate the Gaia EDR3 proper motions of Antlia 2 using our own selection criteria and compare it to the range needed to produce the requisite low pericenter orbits. Since Gaia EDR3 has significantly less error, our results should be less sensitive to selection criteria. By exploring how this updated proper motion calculations affect the orbit, we can reevaluate Antlia 2's dynamical effect on the gas disk of the Milky Way.

*Keywords:* Antlia 2, Galactic dynamics

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## 1. Introduction

The interactions between the Milky Way and nearby dwarf galaxies are crucial to understanding the formation and structure of the universe. The  $\Lambda$  Cold Dark Matter ( $\Lambda$ CDM) model predicts that galaxies like the Milky Way form through a series of merging and accretion events involving smaller systems. Based on this hierarchical cosmological model, the Milky Way should have accreted  $\sim 100 - 200$  satellite galaxies from the past 12 Gyr (Bullock and Johnston, 2005). Galaxy formation processes are simulated with distinctions between the evolution of visible and dark matter in these satellites, which is essential to modeling a stellar halo that is similar to that of the Milky Way and matches its observed number

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10 of surviving satellites. Stars in the inner halo, outer halo, and stars that were affected by  
11 disruption events are all expected to have different chemical compositions, so understanding  
12 how and what the Milky Way interacted with in the past can refine our hierarchical model  
13 of cosmology (Bullock and Johnston, 2005).

14 The outer Galaxy is in particular an ideal environment for studying dwarf galaxy interac-  
15 tions. Large perturbations in the outer Galaxy can be more cleanly attributed to external  
16 perturbers (for regions beyond the stellar disk). The outer HI disks of galaxies are colder  
17 than the stars (and therefore more responsive to perturbations), are more extended than  
18 the stellar disk, and thereby can act as an effective calorimeter for gravitational interactions  
19 (Chakrabarti and Blitz, 2009). A detailed map of the surface density of neutral hydrogen  
20 in the Milky Way revealed perturbations in the outer disk (Levine et al., 2006). These per-  
21 turbations could not be produced in a purely isolated context; earlier work found that the  
22 observed HI disturbances could be caused by a dark sub-halo that tidally interacted with  
23 the Milky Way disk (Chakrabarti and Blitz, 2009). This perturber was estimated to have a  
24 1:100 mass ratio with orbital pericenter  $\sim 10$  kpc (Chakrabarti and Blitz, 2009) at a current  
25 radial distance of  $\sim 130$  kpc.

26 The *Gaia* satellite has produced a wealth of data on the Milky Way. The release of *Gaia*  
27 DR-2 gave access to high quality proper motion measurements which were used to discover  
28 the Antlia 2 dwarf galaxy (Torrealba et al., 2019). Antlia 2 was dubbed a “hidden giant”  
29 because although it has a similar half-light radius as the Large Magellanic Cloud, it is about  
30 4000 times fainter. Its location at a low galactic latitude behind the Milky Way’s central  
31 disk coupled with its dim aspect are likely responsible for it not having been detected in  
32 previous surveys. Intriguingly, the  $\Lambda$ CDM model proposes that dark matter sub-halos often  
33 contain very dim dwarf galaxies, and Antlia 2 is at a radial location that matched previous  
34 predictions of where a dwarf galaxy drove ripples in the outer disk (Chakrabarti and Blitz,  
35 2009). Furthermore, the orbit of Antlia 2 is nearly coplanar to the Galactic disk. If Antlia  
36 2 was responsible for the perturbations in the outer disk, its proper motions would be  
37 constrained to those that would give a lower pericenter (Chakrabarti et al., 2019). Using  
38 *Gaia* EDR3, we will obtain proper motion calculations with lower error and reexamine Antlia  
39 2’s orbital distribution and pericenters to compare them to those predicted in Chakrabarti  
40 et al. (2019).

## 41 2. Method

42 To ensure that our methods are robust across both data releases, we reproduce the orbital  
43 distributions using DR-2 proper motion calculations (Torrealba et al., 2019) (Chakrabarti  
44 et al., 2019). Next, we incorporate the EDR3 proper motions calculated by McConnachie  
45 and Venn (2020) to compare results across data releases.

46 Once we have the location and proper motions of the center of Antlia 2, these three-  
47 dimensional positions and velocities are used as initial conditions for the equation of motion  
48 (Besla et al., 2007). We take into account the gravitational potential of the Milky Way and

49 the dynamical friction due to the passage of Antlia 2 through the dark matter halo of the  
 50 Milky Way:

$$\ddot{\mathbf{r}} = \frac{\partial}{\partial \mathbf{r}} \phi_{MW}(|\mathbf{r}|) + \frac{\mathbf{F}_{DF}}{M_{SAT}} \quad (1)$$

51 where  $\phi_{MW}$  is the gravitational potential of the Milky Way,  $\mathbf{r}$  is the position vector of Antlia  
 52 2 with respect to the galactic center,  $\mathbf{F}_{DF}$  is the dynamical friction term, and  $M_{SAT}$  is the  
 53 mass of Antlia 2.

54 To consider the orbit of Antlia 2, we must infer its mass. There exists a relationships  
 55 between the stellar mass and stellar metallicity of galaxies; higher-mass galaxies are better  
 56 at retaining their metals, while lower-mass galaxies lack the gravitational influence to prevent  
 57 losing their metals to supernova winds, stellar winds, and galaxy-scale feedback. Based on  
 58 DR-2 data, Antlia 2 was reported to have a mean metallicity  $[\text{Fe}/\text{H}] = -1.39$  (Torrealba et al.,  
 59 2019), which by the mass-metallicity relation (Kirby et al., 2013) should correspond to a  
 60 stellar mass of  $\sim 10^7 M_{\odot}$ . Then, a relationship between star formation rate and a satellite  
 61 galaxy’s pre-infall halo mass (Read and Erkal, 2019) was used to derive halo mass from  
 62 stellar mass. The satellite mass of Antlia 2 was inferred to be  $10^{10} M_{\odot}$  (Chakrabarti et al.,  
 63 2019). However, a more recent analysis claims this metallicity was an overestimate, with the  
 64 updated metallicity of Antlia 2 at  $[\text{Fe}/\text{H}] = -1.77$  (Ji et al., 2021). This newly reported  
 65 metallicity corresponds to a substantially smaller satellite mass of Antlia 2, so in Figure 1  
 66 we use the original satellite mass  $10^{10} M_{\odot}$  reported in Chakrabarti et al. (2019) and compare  
 67 it to orbits with smaller satellite masses that would correspond to lower metallicities.

68 It is important to consider the satellite mass of Antlia 2 because of how it affects our  
 69 calculation of the drag force to due dynamical friction. Dynamical friction (DF) occurs when  
 70 moving bodies gravitationally interact with surrounding matter in space and lose momentum  
 71 and energy. A massive object like Antlia 2 moves through particles and attracts them  
 72 towards itself. As the object continues moving, the particles are more densely concentrated  
 73 behind the object than in front, which results in a net drag force. The dynamical friction  
 74 force is proportional to the square of the satellite mass Besla et al. (2007), so a smaller  
 75 object loses less energy to friction and travels through a lower apocenter orbit.

76 This can be seen in Figure 1 where the McConnachie and Venn (2020) proper motion  
 77 measurements of Antlia 2 are integrated in four cases: (a) without dynamical friction, (b)  
 78 including dynamical friction with satellite mass  $M_{SAT} = 1 \times 10^9 M_{\odot}$ , (c)  $M_{SAT} = 3 \times$   
 79  $10^9 M_{\odot}$ , (d)  $M_{SAT} = 5 \times 10^9 M_{\odot}$ , and the earlier inferred Antlia 2 mass  $M_{SAT} = 1 \times 10^{10} M_{\odot}$   
 80 (Chakrabarti et al., 2019). We select these masses to compare the original satellite mass  
 81  $10^{10} M_{\odot}$  reported in Chakrabarti et al. (2019) and the a few smaller satellite masses that  
 82 would correspond to updated lower metallicities. As expected, the orbit not accounting  
 83 for dynamical friction has the lowest apocenter orbit and apocenter increases with satellite  
 84 mass.

85 To solve the equation of motion, we select a Milky Way potential  $\phi_{MW}$  and numerically

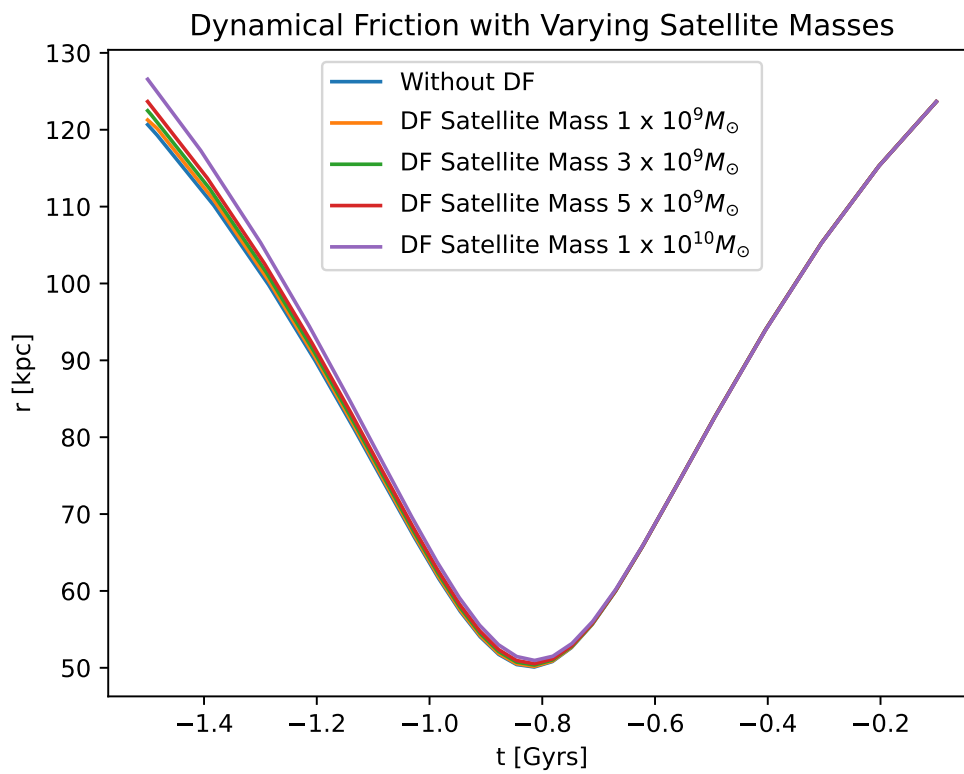


Figure 1: Radial distance from the center of the Milky Way plotted as a function of time. Orbital integrations were calculated in a matched Hernquist potential highlighting the effect of dynamical friction (DF) with varying satellite masses. A more massive satellite loses more energy to dynamical friction, which means it came from an orbit with a higher apocenter.

86 integrate backwards in time to solve for the orbits using an 8th order Runge-Kutta method  
 87 (Chang and Chakrabarti, 2011).

88 The Milky Way potential depends on the mass distribution of dark matter throughout the  
 89 galaxy. We assume that the dark matter halo of the Milky Way is static and spherically  
 90 symmetric. The Hernquist (1990) and Navarro et al. (1997) (NFW) profiles model the dark  
 91 matter distribution in the galaxy as a function of radius. The Hernquist profile is given by

$$\rho_{Hern}(r) = \frac{M}{2\pi} \frac{a}{r(r+a)^3}, \quad (2)$$

92 where  $a$  is the scale radius. The NFW profile slightly differs from Hernquist, i.e.

$$\rho_{NFW}(r) = \frac{\rho_0}{\frac{r}{r_s} \left(1 + \frac{r}{r_s}\right)^2} \quad (3)$$

93 where  $\rho_0$  is the critical density and  $r_s$  is the NFW scale length

94 We match the Hernquist profile to the NFW profile in the inner regions as in Springel et al.  
 95 (2005) by setting the total mass of the Hernquist profile equal to the mass contained within  
 96 the virial radius  $r_{200}$  of an NFW-halo and the densities equal to each other for  $r \ll r_{200}$ . To  
 97 do so, we relate the NFW concentration index  $c = r_{200}/r_s$  to the Hernquist scale radius  $a$ :

$$a = r_s \sqrt{2[\ln(1+c) - c/(1+c)]} \quad (4)$$

98 For large  $r$ , the NFW profile drops off at  $\rho_{NFW} \propto r^{-3}$ , while the Hernquist profile drops off  
 99 at  $\rho_{Hern} \propto r^{-4}$ . Unlike the NFW profile, the total mass of the Hernquist profile converges,  
 100 allowing us to model isolated halos without truncating the distribution. Since varying the  
 101 total mass of the distribution will significantly affect a satellite's orbit, we reproduced the  
 102 plots for orbital distributions and their mass dependence in Chakrabarti et al. (2019) with  
 103 Gaia DR-2 data. Assuming the system of Antlia 2 and the Milky Way satisfies the virial  
 104 theorem, we refer to the relationship between virial mass, velocity, and radius given in  
 105 Springel and White (1999):

$$v_{200}^2 = \sqrt{\frac{GM_{200}}{R_{200}}} \quad (5)$$

106 Higher values of  $v_{200}$  correspond with higher masses  $M_{200}$ , and a higher Milky Way mass  
 107 means the satellite is more tightly bound, so the calculated orbits should have lower peri-  
 108 centers.

109 We performed the integration with various virial velocities ranging from  $v_{200} = 160$  km/s,  
 110 180 km/s, and 200 km/s. This is corresponding to virial masses  $M_{200} = 1.24 \times 10^{12} M_\odot$ ,  
 111  $1.57 \times 10^{12} M_\odot$ , and  $1.93 \times 10^{12} M_\odot$ , which is consistent with expectations from the literature  
 112 (Chakrabarti et al., 2019). We took 1000 proper motion samples from a normal distribution  
 113 based on the mean and standard deviation of the proper motion of Antlia 2. To recreate the

Table 1: Mean EDR3 pericenters for orbital integrations in various density profiles, Milky Way masses, and dynamical friction considerations. Hernquist-NFW denotes the matched Hernquist profile while NFW denotes a pure NFW density profile.

Density Profile	Dynamical Friction?	$v_{200}$ [km/s]	$M_{200}$ [ $M_{\odot}$ ]	$R_p$ [kpc]
Hernquist-NFW	N	160	$1.24 \times 10^{12}$	$50.3 \pm 4.3$
Hernquist-NFW	Y	160	$1.24 \times 10^{12}$	$51.4 \pm 4.3$
Hernquist-NFW	N	180	$1.57 \times 10^{12}$	$41.8 \pm 3.4$
Hernquist-NFW	Y	180	$1.57 \times 10^{12}$	$42.7 \pm 3.4$
Hernquist-NFW	N	200	$1.93 \times 10^{12}$	$35.5 \pm 2.7$
Hernquist-NFW	Y	200	$1.93 \times 10^{12}$	$36.2 \pm 2.9$
Pure NFW	N	160	$1.24 \times 10^{12}$	$57.2 \pm 4.6$
Pure NFW	Y	160	$1.24 \times 10^{12}$	$58.6 \pm 4.7$
Pure NFW	N	180	$1.57 \times 10^{12}$	$48.0 \pm 3.8$
Pure NFW	Y	180	$1.57 \times 10^{12}$	$48.8 \pm 3.9$
Pure NFW	N	200	$1.93 \times 10^{12}$	$41.0 \pm 3.1$
Pure NFW	Y	200	$1.93 \times 10^{12}$	$41.8 \pm 3.2$

114 results from *Gaia* DR-2, we used both the proper motions given in Torrealba et al. (2019)  
 115 and Chakrabarti et al. (2019) and backward integrating the orbits in the matched Hernquist  
 116 potential to create histograms of the pericenter distributions.

117 We then used *Gaia* EDR3 proper motion measurements of Antlia 2 as reported recently  
 118 in (McConnachie and Venn, 2020) and produced the pericenter distributions. Since these  
 119 proper motion measurements are more accurate than those from DR-2, their corresponding  
 120 distributions should have lower standard deviations.

### 121 3. Results and Discussion

122 We proceed to using *Gaia* EDR3 proper motions of Antlia 2 calculated by McConnachie  
 123 and Venn (2020). We sampled 1000 proper motions from a normal distribution based on  
 124 the mean and standard deviation of the proper motion measurements, then integrated all  
 125 of them to create pericenter distributions. We repeated this for various density profiles and  
 126 dynamical friction considerations for virial velocities  $v_{200} = 160 - 200$  km/s.

127 Table 1 lists the mean pericenters for these orbital integrations. As expected, higher virial  
 128 velocities correspond to lower mean pericenters and the distributions using EDR3 data have  
 129 lower standard deviations.

130 We also overlay the pericenter distributions to compare the results across density profiles and  
 131 dynamical friction considerations. Figures 2 and 3 are pericenter distributions in a matched  
 132 Hernquist profile without dynamical friction, a Hernquist profile with dynamical friction,  
 133 and a pure NFW profile without dynamical friction. Figure 2 is based on DR-2 proper  
 134 motions (Chakrabarti et al., 2019) while Figure 3 uses EDR3 proper motions (McConnachie

135 and Venn, 2020). Clearly, the DR-2 distributions are wider, indicating that more accurate  
136 EDR3 proper motion measurements have given us a more accurate picture of the orbit of  
137 Antlia 2. It is also worth noting that the EDR3 distributions are significantly higher than  
138 those derived from DR-2 calculations.

139 For cases involving dynamical friction, the satellite mass was set to  $10^{10}M_{\odot}$ , the mass of  
140 Antlia 2 reported in Chakrabarti et al. (2019). For all integrations in Table 1, accounting  
141 for dynamical friction did not make a significant difference in mean pericenter. This aligns  
142 with our expectations since accounting for dynamical friction should have a larger effect on  
143 the apocenter of the orbit. Using the pure NFW profile instead of the matched Hernquist  
144 profile seems to result in slightly higher pericenters, but the difference is not significant.

#### 145 4. Conclusions

146 The large planar disturbances in the outer HI disk of our Galaxy (Levine et al., 2006) have  
147 been a long-standing puzzle. Earlier dynamical analysis found that they could be produced  
148 by a massive dwarf galaxy on a close approach (Chakrabarti and Blitz, 2009). The recent  
149 discovery of the Antlia 2 dwarf galaxy from Gaia DR-2 (Torrealba et al., 2019) was a  
150 compelling candidate (Chakrabarti et al., 2019) to explain these disturbances. Motivated  
151 by the release of Gaia EDR3, we revisited the earlier analysis of the DR-2 data (for which  
152 the proper motions had substantially larger error bars) by Chakrabarti et al. (2019). We  
153 have checked that we recover the prior results for the pericenter distributions using DR-2  
154 proper motion calculations from Torrealba et al. (2019) and Chakrabarti et al. (2019). As  
155 expected, the EDR3 proper motions are much more precise than DR-2, and here we have  
156 used orbit integration calculations to find that the the EDR3 proper motions (McConnachie  
157 and Venn, 2020) imply larger pericenters on average relative to DR-2. Recent work (Ji et al.,  
158 2021) indicates that the discovery paper on Antlia 2 (Torrealba et al., 2019) overestimated  
159 the metallicity of Antlia 2, which would suggest a lower progenitor mass for Antlia 2 than  
160 was considered earlier (Chakrabarti et al., 2019).

161 At face value, these newer results seem to suggest that Antlia 2 may not be the long-sought  
162 after culprit to explain the disturbances in the outer HI disk. However, our orbit integration  
163 calculations here did not include the effect of the LMC. Recent work (Ji et al., 2021) suggests  
164 that (even within an approximate framework) including the effect of the reflex motion of the  
165 LMC will produce lower pericenters for Antlia 2 that agree more closely with previous results.  
166 The potentials that we have considered here are spherically symmetric and the inclusion of  
167 a disk potential can also be expected to increase the tidal effect. More fundamentally, the  
168 HI map produced by Levine et al. (2006) *assumed* kinematic distances. It will be interesting  
169 to see whether a more accurate HI map produced using asteroseismic distances (Auge et al.,  
170 2020) will still yield large planar disturbances as in the original HI map constructed by  
171 Levine et al. (2006).

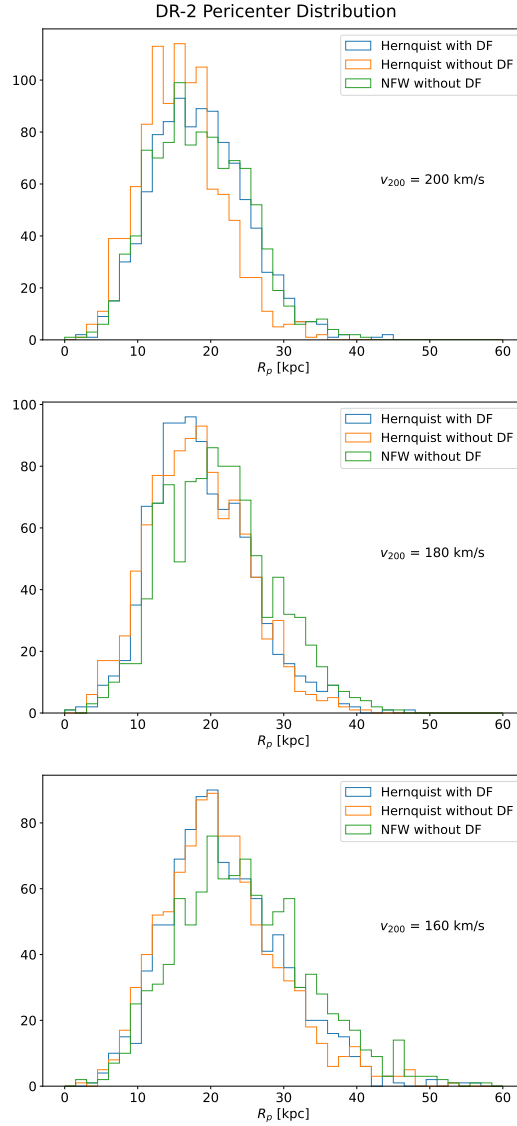


Figure 2: Pericenter distributions using 1000 samples from proper motion calculations made by Chakrabarti et al. (2019) with varying virial masses. Orbits were integrated in a matched Hernquist potential with dynamical friction, a matched Hernquist potential without dynamical friction, and a pure NFW potential without dynamical friction. The step histograms were plotted together to compare the effects on pericenter distributions. Compared to the matched Hernquist profile without dynamical friction (orange), the NFW profile (green) results in slightly higher pericenters within error bars. Taking into account dynamical friction (blue) results in slightly lower mean pericenters, but the effect is not significant.



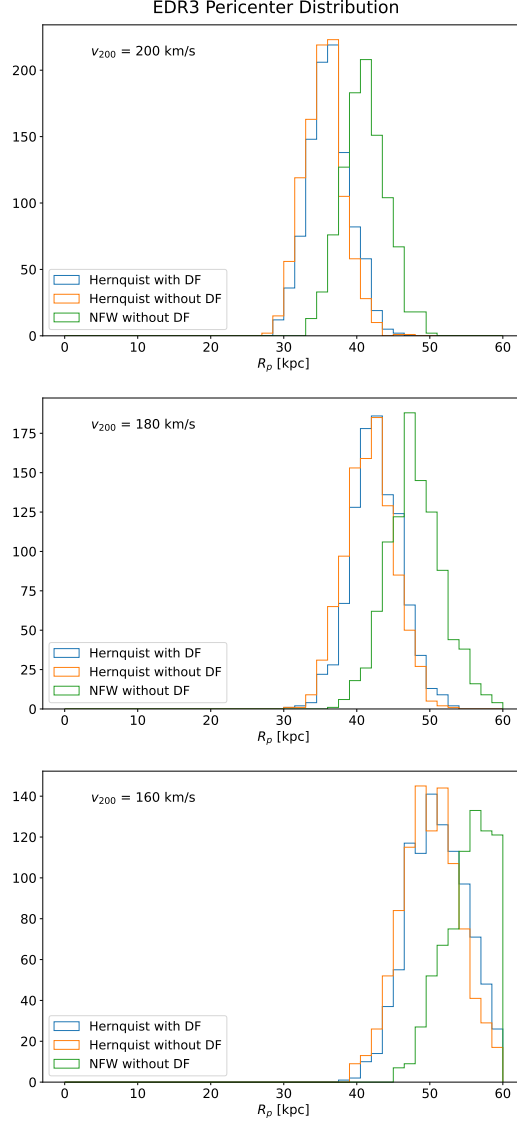


Figure 3: EDR3 pericenter distributions using 1000 samples from proper motion calculations made by McConnell and Venn (2020) with varying virial masses. We used the same criteria as Figure 2 to integrate the orbits and plot step histograms. The relationship varying density profiles and dynamical friction are the same across both DR-2 and EDR3 data. However, the pericenter distributions calculated using EDR3 data has significantly higher mean pericenters. The EDR3 histograms are also much narrower, which is a result of better proper motion measurements allowing us to get a more accurate picture of Antlia 2’s orbit.

## 172 5. Ongoing and Future Work

173 We are working on using our own selection criteria to independently recalculate the proper  
174 motions of Antlia 2. To filter out foreground Milky Way stars and isolate the member stars  
175 of Antlia 2, we have a number of tools at our disposal. We first choose stars that are close to  
176 the center of Antlia 2 as reported in (Torrealba et al., 2019) ( $\alpha = 143.8868$ ,  $\delta = -36.7673$ ) by  
177 querying 400,000 stars within 5 degrees in the *Gaia* archive. Next, we plot  $\mu_\alpha \cos \delta$  against  
178  $\mu_\delta$  and look for a cluster with similar proper motions. Lastly, we know that the stars in  
179 Antlia 2 should be a similar age, so we plot their luminosities ( $G$ ) vs effective temperature  
180 ( $B_p - R_p$ ) on a Hertzsprung-Russell diagram and compare them to theoretical isochrones.  
181 Choi et al. (2016) created theoretical isochrones using a 1D stellar evolution model from  
182 the pre-main sequence to the end of hydrogen burning (or carbon burning for more massive  
183 stars) and recorded  $G$ ,  $B_p$ ,  $R_p$ , and the age of each simulated star. By selecting a specific age  
184 and plotting these theoretical isochrones on top of the HR diagram of Antlia 2 candidates,  
185 we can narrow down member stars to those that are of similar age.

186 To compare our methods across data sets, we first reproduce the *Gaia* query and selection  
187 from (Chakrabarti et al., 2019). We queried 400,000 stars from *Gaia* DR-2, then made the  
188 same cuts as Chakrabarti et al. (2019): stars with parallax  $\pi < 0.25$ , located within 1.5  
189 degrees from the center of Antlia 2, and with proper motion magnitude under 0.8 km/s.  
190 Figure 4 plots the queried stars on a color-magnitude diagram and proper motion space.  
191 We then queried stars from EDR3 using the same criteria to produce an analogous colour  
192 magnitude and proper motion diagrams in Figure 5. The longer integration time of EDR3  
193 allowed for the detection of fainter stars and more accurate measurements. When comparing  
194 Figures 4 and 5, the EDR3 diagrams proper motion space has darker spots within in a smaller  
195 region, indicating more stars detected and less error in their proper motions.

196 Next, we will use an ensemble Markov Chain Monte Carlo (MCMC) sampler emcee Foreman-  
197 Mackey et al. (2013) to independently determine the proper motion of Antlia 2. We will  
198 then explore how different selection filters affect the resulting proper motions calculation,  
199 such as varying search radius, isochrone files, and proper motion cuts.

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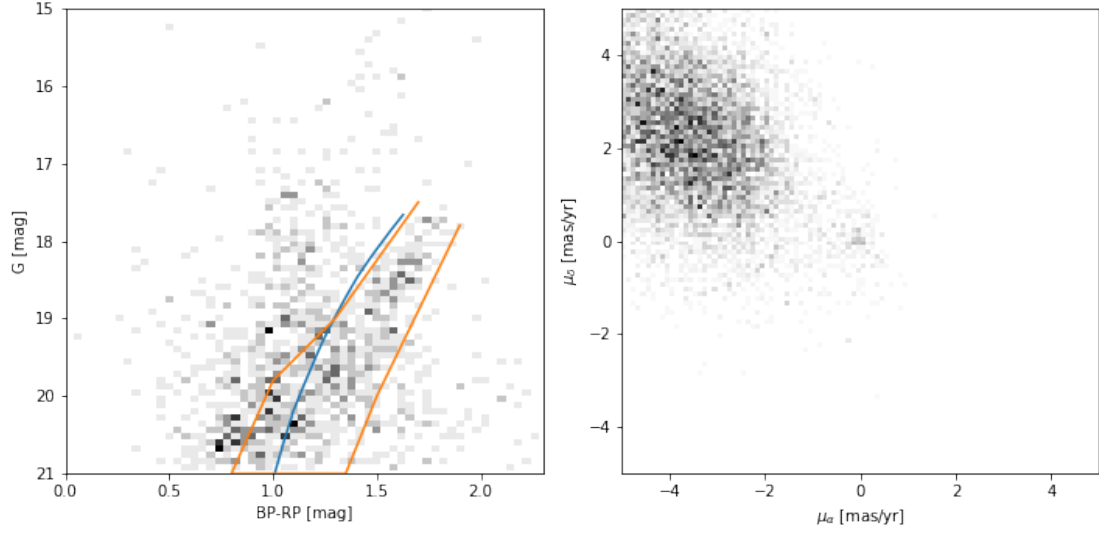


Figure 4: Reproducing Torrealba et al. (2019) CMD and proper motion graphs using Gaia DR-2. Stars were filtered by parallax  $\pi < 0.25$ , located within 1.5 degrees from the center of Antlia 2, and with proper motion magnitude under 0.8 km/s

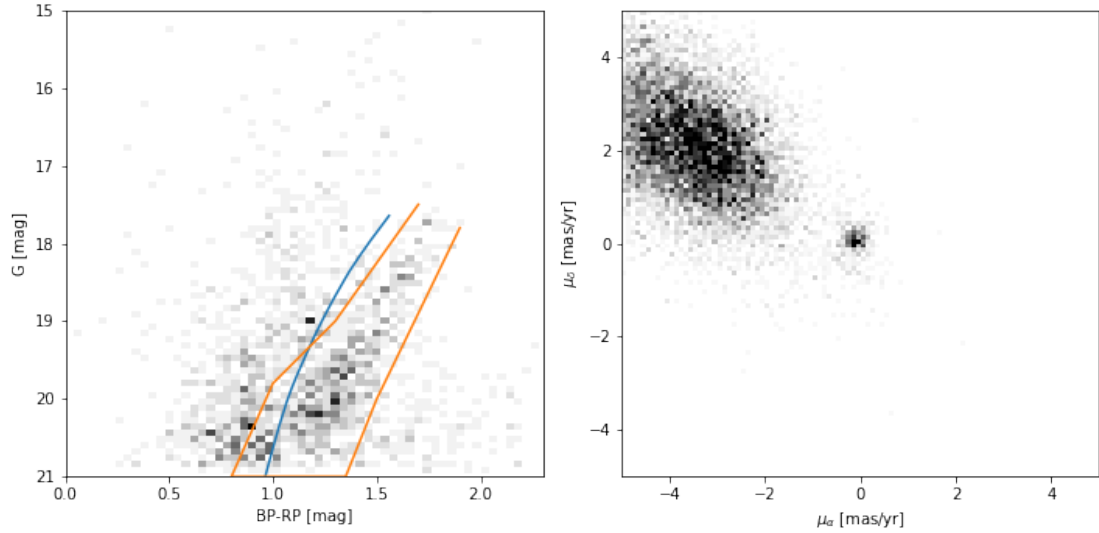


Figure 5: CMD and proper motion graphs using *Gaia* EDR3. Due to the longer integration time, EDR3 was able to detect fainter stars, which can be seen as darker spots in the proper motion histogram. A theoretical isochrone file corresponding to  $[Fe/H] = -1.75$  was used to reflect the updated lower metallicity.

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251 **Appendix**

252 To develop the requisite understanding of Python, I completed a series of small projects  
253 to learn basic data analysis skills. These included plotting a circle, creating a scatterplot  
254 between two axes, a chi square goodness of fit test, creating histograms, reading and writing  
255 to a file, labeling axes, using colors, and using subplots within a plot.